# Ordinary Exam <br> DATA STRUCTURES AND ALGORITHMS DVG B03 

130115 08:15-13:15

Course Coordinator: Donald F. Ross
Help Material: A Dictionary from the student's home language to English.
*** OBS ***

Students who have studied the course as from (>=) Autumn Term 2006

## Grading Levels:

Course: Max 60p, pass with special distinction 50p, pass with distinction 40p, pass 30p (of which a minimum 15p from the exam, 15p from the labs)
Exam: $\quad$ Max 30p, grade 5: $26 \mathrm{p}-30 \mathrm{p}$, grade 4: $21 \mathrm{p}-25 \mathrm{p}$, grade 3: $15 \mathrm{p}-20 \mathrm{p}$
Labs: Max 30p, grade 5: $26 \mathrm{p}-30 \mathrm{p}$, grade $4: 21 \mathrm{p}-25 \mathrm{p}$, grade $3: 15 \mathrm{p}-20 \mathrm{p}$

Students who have studied the course before (<) Autumn Term 2006
Grading Levels:
Course: Max 60 p, pass with special distinction 50 p, pass with distinction 40 p, pass 30 p (of which a minimum 20p from the exam, 10p from the labs)
Exam: $\quad$ Max 40p, grade 5: $34 \mathrm{p}-40 \mathrm{p}$, grade 4: $27 \mathrm{p}-33 \mathrm{p}$, grade 3: 20p-26p
Labs: Max 20p, grade 5: $18 \mathrm{p}-20 \mathrm{p}$, grade $4: 14 \mathrm{p}-17 \mathrm{p}$, grade 3: $10 \mathrm{p}-13 \mathrm{p}$
Write legibly - read all questions carefully

## (1) Give a short answer to each of the following questions:-

(a) Show the relationship between a binary search tree, a complete tree and a full tree with the help of a Venn-diagram from set theory.
(b) What is the maximum load factor in hashing with quadratic probing as the collision management technique which guarantees that a space can always be found?
(c) What is "big-O"?
(d) What does Warshall's algorithm do?
(e) Give a definition of an AVL-tree.
(f) Which grammatical class in natural language corresponds to a relation in the Entity Relationship model?
(g) Which algorithm requires a DAG as a starting point?
(h) Which data structures are ordered?
(i) Which algorithm is $\mathrm{O}\left(\mathrm{n}^{3}\right)$ ?
(j) Give a definition of a recursive function.

## Total 5p

## (2) Abstraction

Discuss in detail why abstraction is so important in data structures. Are there any possible disadvantages to abstraction? Which 3 definitions of the term abstraction have we used in this course?

$$
\mathbf{5 p}
$$

## (3) Sequence

(a) Give a recursive definition of a sequence.
(b) From your definition in (a) above, write recursive pseudo code to count up the number of elements in a sequence
State all assumptions.
Give an example of how your code works.
(2p)
(c) From your definition in (a) above, write recursive pseudo code to add an element to a sequence in increasing (sorted) order. Assume that a function called Cons which adds an element to the head of the list already exists.
Cons: element x list $\rightarrow$ list.
State all assumptions.
Give an example of how your code works.
(4) General questions - give a detailed answer with an example
(a) What is double hashing?
(b) What is a stack used for?
(c) How is a general tree transformed to a binary tree?
(d) How does the add function work in a heap?
(e) Describe a solution to the TSP-problem. TSP = Travelling Salesman Problem.

## Total 5p

(5) Graph - Dijkstra + SPT

Extend Dijkstra's algorithm below in order to save and show the SPT. (SPT: Shortest Path Tree).

```
Dijkstra ()
{ S={a}
    for (i in 2..n) D[i] = C[a,i] -- initialise D
    for (i in 1..(n-1)) {
    choose w in V - S such that D[w] is a minimum
    S = S + {w}
    foreach (v in V-S) D[v] = min(D[v], D[w]+C[w,v])
    }
    }
```

Apply your extended version of the algorithm to the following directed graph:-
(a, b, 13), (a, d, 12), (a, e, 20), (b, c, 60), (c, e, 50), (d, c, 30), (d, e, 40)
Start at node "a".
Show each step in your calculation.
State all assumptions and show all calculations and intermediate results.
Draw each step in the construction of the STP-i.e. show the nodes and which edges are added and subsequently removed.

Total 5p
(6) Graph - Prim's algorithm

Apply the version of Prim's algorithm given below to the undirected graph:-
(a-6-b, a-3-c, a-7-d, b-1-c, b-12-e, c-4-d, c-5-e, c-9-f, d-3-f, e-8-f).
Start with node "a".
State all assumptions and show all calculations and intermediate results.
(3p)
Explain the principles behind Prim's algorithm.
Use the example above in your explanation.
(2p)
Prim ( node $v$ ) -- $v$ is the start node
\{ $\mathrm{U}=\{\mathrm{v}\}$; for i in $(\mathrm{V}-\mathrm{U})\{$ low-cost $[\mathrm{i}]=\mathrm{C}[\mathrm{v}, \mathrm{i}] ;$ closest $[\mathrm{i}]=\mathrm{v} ;\}$
while (!is_empty (V-U) ) \{
$\mathrm{i}=\mathrm{first}(\mathrm{V}-\mathrm{U}) ; \mathbf{m i n}=\operatorname{low}-\operatorname{cost}[\mathrm{i}] ; \mathrm{k}=\mathbf{i}$;
for $\mathbf{j}$ in (V-U-k) if (low-cost[j] < min) \{min = low-cost[j]; $k=j ;\}$
display(k, closest[k]);
$\mathbf{U}=\mathbf{U}+\mathbf{k}$
for $\mathbf{j}$ in (V-U) if ( $\mathbf{C}[\mathbf{k}, \mathbf{j}]$ < low-cost $[\mathbf{j}])$ ) \{low-cost[j]=C[k,j]; closest[j]=k; \} \}
\}

Total 5p

